

# Exercise Part 6

## Coding Theory, Finite Fields, and AES

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### 1 Wednesday 29 October 2014

**Exercise 1** Write the following numbers in Hexadecimal:

1. 321
2. 1519

**Exercise 2** Write the following numbers in Octal:

1. 321
2. 721
3. 1519

**Exercise 3** Write the following hexadecimal numbers in decimal:

1. 17A2

**Exercise 4** Write the following octal numbers in decimal:

1. 077
2. 03771

**Exercise 5** Write down the decryption keys for the following transposition encryption keys:

1. (4, 5, 1, 3, 2)
2. (7, 4, 6, 1, 5, 3, 2)

**Exercise 6** Find the inverse matrices over  $\mathbb{Z}^5$  for

$$\begin{bmatrix} 1 & 0 & 4 \\ 0 & 1 & 0 \\ 3 & 0 & 1 \end{bmatrix} \quad (1)$$

You can use Gaussian elimination in the same way as you would over the reals.

## 2 Tuesday 4 November 2014

**Exercise 7** Calculate

1. Over  $\mathbb{Z}_2$ :  $x^8 + x^6 + x^5 + x^2 + x + 1 \pmod{x^4 + 1} =$
2. Over  $\mathbb{Z}_2$ :  $x^6 + x^4 + x^3 + 1 \pmod{x^4 + x + 1} =$
3. Over  $\mathbb{Z}_3$ :  $x^5 + 2x^4 + x^2 + 2 \pmod{x^3 + 2x + 1} =$

**Exercise 8** Calculate

1. Over  $\mathbb{Z}_2$ :  $(x^3 + x + 1)(x + 1) \pmod{x^2 + x + 1}$
2. Over  $\mathbb{Z}_2$ :  $(x^3 + x^2 + 1)(x^4 + x^3 + 1) \pmod{x^2 + x + 1}$
3. Over  $\mathbb{Z}_3$ :  $(x^2 + 2x + 1)(x^4 + x^3 + 2x + 2) \pmod{x^3 + 2x + 1}$

## 3 Thursday 6 November 2014

**Exercise 9** Consider the following matrices:

$$A = \begin{bmatrix} 1 & 0 & 0 & 1 \\ 1 & 1 & 0 & 1 \\ 1 & 0 & 1 & 1 \\ 0 & 0 & 0 & 1 \end{bmatrix} \quad \text{over } \mathbb{Z}_2,$$

$$A = \begin{bmatrix} 1 & 2 & 0 \\ 2 & 2 & 1 \\ 1 & 1 & 1 \end{bmatrix} \quad \text{over } \mathbb{Z}_3,$$

$$A = \begin{bmatrix} 1 & 2 & 0 \\ 3 & 4 & 1 \\ 1 & 0 & 2 \end{bmatrix} \quad \text{over } \mathbb{Z}_5,$$

Find  $A^{-1}$ .

## 4 Friday 7 November 2014